FORMAL METHODS Fall 2011 (last revised: 8 sep 2011)

COURSE LING 461/661 1085 Docteur-Penfield rm. 002 TIME: MWF 8h35–9h25 INSTRUCTOR

Brendan S. Gillon 1085 Docteur-Penfield rm. 119 OFFICE HOURS: t.b.a. and by appointment tel. no.: 514 398 4868

## AIM OF THE COURSE:

The aim of the course is to prepare students so that they can understand the mathematics used in the literature in syntax, but especially in semantics, and acquire a degree of mathematical maturity. Stress is put on understanding fundamental concepts and doing informal proofs. Topics covered are: sets and operations on them, family of sets and operations on them, mathematical induction, relations and functions, partial orders and lattices.

## COURSE MATERIAL:

- Abbott, James C. 1969 *Sets, lattices and Boolean algebras.* Prentice-Hall.
- Stoll, Robert R. 1963 Set theory and logic. Dover Publications.
- Gillon, Brendan S. 2008 Introduction to sets, orders and lattices. Unpublished manuscript.

EVALUATION: 10 problem sets (10% each)

## PROCEDURES:

- NO LATE PROBLEM SETS WILL BE ACCEPTED. Each problem set must be turned in at the beginning of the class on its due date.
- NO MAKE-UP EXAMINATIONS WILL BE GIVEN to anyone who does not have a certified medical excuse.
- NO ANSWER TO ANY GRADED PROBLEM OR EXAMINATION QUESTION WILL BE RE-ASSESSED, unless:
  - 1. the answer is written in ink;
  - 2. it has not been written over; and
  - 3. the answer is clearly marked as such.
- Assignments and examins be written either in ENGLISH or in FRENCH.

McGill University values academic integrity. Therefore all students must understand the meaning and consequences of cheating, plagiarism and other academic offences under the code of student conduct and disciplinary procedures. (See www.mcgill.ca/integrity for more information.)

L'Université McGill attache une haute importance à l'honnêteté académique. Il incombe par conséquence à tous les étudiants de comprendre ce que l'on entend par tricherie, plagiat et autres infractions académiques, ainsi que les conséquences que peuvent avoir de telles actions, selon le Code de conduite de l'étudiant et des procédures disciplinaires. (Pour de plus amples renseignements, veuillez consulter le site www.mcgill.ca/integrity.)

## SYLLABUS

| week 1 (2 Sep):  |                                   |  |
|------------------|-----------------------------------|--|
| week 2 (9 Sep):  | sets                              | Stoll 1963 ch. 1.1–1.5<br>Abbott 1963 ch. 2.10–2.11<br>Gillon 2008 ch. 1, ch. 2      |
| week 3 (16 Sep): | informal axiomatic set theory     | Abbott 1969 ch. 1<br>Stoll 1963 ch. 7.1–7.5  |
| week 4 (23 Sep): | relations<br>and functions        | Abbott 1969 ch. 2.1–2.4<br>Stoll 1963 ch. 1.6–1.9<br>Gillon 2008 ch. 3, ch. 5, ch. 6 |
| week 5 (30 Sep): | families of sets<br>and induction | Abbott 1969 ch. 2.14<br>Stoll 1963 ch. 1.10<br>Gillon 2008 ch. 4.                    |
| week 6 (7 Oct):  | orders                            | Abbott 1969 ch. 4.1–4.4<br>Stoll 1963 ch. 1.11<br>Gillon 2008 ch. 8                  |
| week 7 (14 Oct): | algebra                           | Stoll 1963 ch. 8.1–8.5<br>Abbott 1969 ch. 2.5–2.9<br>Gillon 2008 ch. 7.5             |
| WEEK 8 (21 Oct): | lattices                          | Abbott 1969 ch. 4.5–4.8<br>Gillon 2008 ch. 9   |
| WEEK 9 (28 Oct): | Boolean algebras                  | Abbott 1969 ch. 6.1–6.3<br>Stoll 1963 ch. 6.1–6.3<br>Gillon 2008 ch. 10              |

| WEEK 10 (4 Nov):  | Boolean algebras | Abbott 1969 ch. 6.4–6.5<br>Gillon 2008 ch. 10                           |
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| week 11 (11 Nov): | Boolean algebras | Abbott 1969 ch. 6.6–6.7<br>Stoll 1963 ch. 6.4–6.5<br>Gillon 2008 ch. 10 |
| week 12 (18 Nov): | Boolean algebras | Abbott 1969 ch. 6.9–6.11<br>Stoll 1963 ch. 6.7<br>Gillon 2008 ch. 10    |
| WEEK 13 (25 Nov): | Boolean algebra  | Stoll 1963 ch. 6.6, 6.8–6.9<br>Gillon 2008 ch. 10                       |