

Incomplete Contracts in Dynamic Games

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Abstract

I develop a dynamic model of costly private provision of public goods where agents can also invest in cost-reducing technologies. Despite the $n+1$ stocks in the model, the analysis is tractable and the (Markov perfect) equilibrium unique. The framework is used to derive optimal incomplete contracts in a dynamic setting. If the agents can contract on provision levels, but not on investments, they invest suboptimally little, particularly if the contract is short-term or close to its expiration date. To encourage sufficient investments, the optimal and equilibrium contract is more ambitious if it is short-lasting, and it is tougher to satisfy close to its expiration date. If renegotiation is possible, such a contract implements the first best. The results have important implications for how to design a climate treaty.

Key words: Dynamic private provision of public goods, dynamic common-pool problems, dynamic hold-up problems, incomplete contracts, renegotiation design, climate change and climate agreements

JEL: D86, H87, Q54, F53

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1. Introduction

This paper develops a dynamic model of private provision of public goods. The agents can also invest in cost-reducing technologies, leading to $n + 1$ stocks, but the analysis is nevertheless tractable. I derive and characterize a unique Markov perfect equilibrium for the noncooperative game as well as for situations where the agents can negotiate and contract on contribution levels. In particular, the optimal and equilibrium contract is described.

The model is general and could fit various contexts. The leading example is climate change, and the results have clear implications for how to design an efficient treaty. Consistent with the model's assumptions, a country can reduce its emission in multiple ways: a short-term solution is to simply consume less fossil fuel today, while a more long-term solution might be to invest in new technologies, such as renewable energy sources or abatement technology. The Kyoto Protocol is a bargaining outcome limiting the countries' emission levels, but it does not specify the extent to which countries should invest or simply reduce its short-term consumption. This distinction would, in any case, be difficult to verify. At the same time, the Protocol is relatively short-lasting, since the commitments expire in 2012. This may reflect the difficulties or costs of committing to the distant future.

All these aspects are in line with the model. To fix ideas, I will refer to the players as "countries" and their contributions as "emissions." The public good, or rather its negative: the public bad, can be interpreted as greenhouse gases. The technology provides a private substitute for polluting, and can be interpreted as renewable energy or abatement technology. The model abstracts from heterogeneities across and within countries as well as the difficulties of motivating participation and compliance. I thus describe an idealized benchmark case that isolates the interactions between negotiated quotas and incentives to invest in technologies.

The real investment cost function may be convex or concave (if there are increasing returns to scale). By assuming it is linear, I prove that the continuation value must be linear in *all* the $n + 1$ stocks. Thus, the payoff-relevant history is represented by a weighted

sum of the stocks. Only one MPE satisfies these conditions, so the MPE is unique. This MPE is stationary and coincides with the unique subgame perfect equilibrium if time were finite but approached infinity. These attractive equilibrium properties hold for every scenario studied in the paper.

First, the noncooperative outcome is characterized. Although the technology is private and investments are selfish, each country's technology stock is, in effect, a public good, since its role is to substitute for the country's contribution to the public bad. If one country happens to pollute a lot, the other countries are, in the future, induced to pollute less since the problem is then more severe. They will also invest more in technology to be able to afford the necessary cuts in emissions. On the other hand, if a country invests a lot in abatement technology, it can be expected to pollute less in the future. This induces the other countries to increase their emissions and reduce their own investments. Anticipating these effects, each country pollutes more and invests less than it would in an otherwise similar static model. This dynamic common-pool problem is thus particularly severe.

Since the MPE is unique, agreements enforced by trigger strategies are not feasible. Instead, I derive the equilibrium outcome assuming the agents can contract on emission levels. For climate agreements, for example, countries may be able to commit at least to the near future, since domestic stakeholders can hold the government accountable if it has ratified an international agreement. Instead of taking a stand on the countries' ability to commit, I derive the equilibrium contract as a function of this ability.

To begin, suppose the time horizon of a contract is represented by the length of "a period" in the model. If there were only one period, contracting on emission levels would be first best since investments in technology are selfish (one country's investment has no spillover effect on the other countries' technologies). With multiple periods, however, the technology stock that survives to the next period is, in effect, a public good. The reason for this is that a hold-up problem arises when the countries negotiate emission levels: if one country has better technology and can cut its emissions fairly cheaply, then its opponents may ask it to bear the lion's share of the burden when collective emissions are reduced. Anticipating this, countries invest less when negotiations are coming up. Thus,

the countries underinvest, particularly if the period is short while the technology is long-lasting. With smaller investments, it is ex post optimal to allow for larger emission levels. On the other hand, since the countries are underinvesting, they would like to encourage more investments and they can do this by negotiating a contract that is tough and allows few emissions. Thus, the best (and equilibrium) contract is tougher and stipulates *lower* emissions compared to the optimum ex post, particularly if the length of the contract is relatively short and the technology long-lasting. Surprisingly, the equilibrium pollution level is identical to the level that would have been first best if investments had been efficient.

If the countries can negotiate and contract on the emission level for several periods, then investments are suboptimally low only at the end of the agreement, since the technology that then remains is, in effect, a public good, thanks to the hold-up problem. Thus, investments decline toward the end of the contract. Anticipating this, and to further motivate investments, the optimal and equilibrium contract becomes tougher to satisfy over time.

However, these contracts are not renegotiation-proof. Once the investments are sunk, countries have an incentive to negotiate ex-post optimal emission levels rather than sticking to an overambitious contract. When renegotiation is possible and cannot be prevented, an investing country understands that it does not, in the end, have to comply with overambitious contracts. Nevertheless, with renegotiation, all investments and emissions are *first best*. Intuitively, emission levels are renegotiated to ex-post optimal levels. Countries with poor technology find it particularly costly to comply with an initial ambitious agreement and will be quite desperate to renegotiate it. This gives them a weak bargaining position and a bad outcome. To avoid this fate, countries invest more in technology, particularly if the initial contract is very ambitious. Taking advantage of this effect, the contract should be tougher if it has a relatively short duration, or if it is close to its expiration date, just as in the case without renegotiation.

Observationally, the outcome of these (re)negotiations is equivalent to a time-inconsistency problem. Repeatedly, the countries make very ambitious promises for future actions. But when the future arrives, they relax these promises while, at the same time, they make

ambitious promises for the future - once again. However, rather than being evidence of a time-inconsistency problem, this behavior implements the first best in this model.

The results have important implications for the optimal design of a climate treaty. First, even if countries can commit to emission quantities and investments are selfish, countries tend to invest too little, particularly for short-term agreements. Second, the optimal treaty should be tougher if it is short-term and, third, it should be tougher close to its expiration date. Finally, efficiency is achieved by long-term agreements that are renegotiated over time. In other words, when negotiating a new treaty, it is better if the default outcome is some existing treaty rather than the noncooperative outcome. This suggests that climate negotiators have something to learn from international trade policy negotiators, since trade agreements are typically long-lasting, although they can expand or be renegotiated over time.

While this paper is more general and emphasizes the benefits of renegotiation, my companion paper, Harstad (2010), assumes quadratic utilities and goes further when studying short-term agreements, whether such an agreement is valuable, and what the optimal agreement length should be. Furthermore, that paper shows that domestic holdup problems interact with the international one, and that the optimal climate treaty design depends on existing R&D policies, and vice versa.

The next section clarifies the paper's contribution to the literature on dynamic games and incomplete contracts. The model is presented in Section 3. When solving the model in Section 4, I gradually increase the possibilities for negotiations and contracts by analyzing (i) no cooperation, (ii) one-period contracts, (iii) multi-period contracts, and (iii) contracts permitting renegotiation. Section 5 allows for technological spillovers and Section 6 discusses other extensions and generalizations. Section 7 concludes, while the appendix contains all proofs.

2. Contributions to the Literature

By developing a dynamic (difference) game permitting incomplete contracts, the paper contributes to the literature on both of these fields.

2.1. Dynamic Games

The private provision of public goods is often studied in differential games (or a difference game, if time is discrete) where each player’s action influences the future stock or state parameter.¹ Given the emphasis on stocks, the natural equilibrium concept is Markov perfect equilibrium.² As in this paper, the typical conclusion is that public goods (bads) are underprovided (overprovided).³

Differential games are, however, often difficult to analyze. This has several implications. First, many authors restrict attention to linear-quadratic functional forms.⁴ Second, while some papers arbitrarily select the linear MPE (e.g., Fershtman and Nitzan, 1991), typically there are multiple equilibria (Wirl, 1996; Tutsui and Mino, 1990). Consequently, many scholars, like Dutta and Radner (2009), manage to construct more efficient nonlinear MPEs.⁵ Third, few bother complicating their model further by adding investments in technologies. One exception is Dutta and Radner (2004), who do explicitly add investments in technology. But since the cost of pollution (as well as the cost of R&D) is assumed to be linear, the equilibrium is “bang-bang” where countries invest either zero or maximally in the first period, and never thereafter.

The first contribution of this paper is the development of a tractable model that can be used to analyze investments as well as emissions. By assuming that technology has a linear cost and an additive impact, I find that the continuation values must be linear in all the $n + 1$ stocks, permitting only a single MPE. This trick sharpens the predictions and simplifies the model tremendously. Potentially, this trick can also be applied when studying other economic problems. In the literature on industry dynamics, for example, analytical solutions are rare and numerical simulations necessary.⁶

¹Thus, such games are subclasses of stochastic games. For overviews, see Başar and Olsder (1999) or Dockner et al. (2000).

²In experiments, players tend toward Markov perfect strategies rather than supporting the best subgame perfect equilibrium (Battaglini et al., 2010).

³This follows if private provisions are strategic substitutes (as in Fershtman and Nitzan, 1991, and Levhari and Mirman, 1980). If they were complements, e.g., due to a discrete public project, efficiency is more easily obtained (Marx and Matthews, 2000).

⁴For a comprehensive overview, see Engwerda (2005).

⁵See also Dockner and Long (1993), Dockner and Sorger (1996), and Sorger (1998).

⁶See the survey by Doraszelski and Pakes (2007). A firm typically overinvests in capacity to get a competitive advantage. While Reynolds (1987) restricts attention to the linear MPE in a linear-quadratic model, simple two-stage games are used by d’Aspremont and Jacquemin (1988) to discuss the benefits of

My second contribution, made possible by the first, is to incorporate incomplete contracts in dynamic games. Few papers allow for policies or negotiation in stochastic games.⁷ In Battaglini and Coate (2007), legislators negotiate spending on "pork" and a long-lasting public good. The equilibrium public-good level is suboptimally but strategically low to discourage future coalitions from wasting money on pork. This mechanism relies on majority rule, however, and the contract incompleteness is related to future policies rather than current investments.

2.2. Contract Theory

By permitting contracts on emissions but not on investments, this paper is in line with the literature on incomplete contracts (e.g., Hart and Moore, 1988). Since I assume investments are selfish in that they affect only the investor's technology stock, contracting on quantity would implement efficiency if there were only one period, or if the contract lasted forever. However, if the countries cannot commit to the end of time, I find that investments are lower if the contract length is short, and that investments decrease toward the end of a contract. To encourage more investments, the optimal and equilibrium contract is tougher to comply with if the contract is short-term or close to its expiration date, particularly if the technology is long-lasting compared to the length of the agreement. These results have not been detected earlier, to the best of my knowledge.

In other dynamic settings, hold-up problems may be solved if the parties can invest while negotiating and agreements can be made only once (Che and Sakovics, 2004), or if there are multiple equilibria in the continuation game (Evans, 2008). Neither requirement is met in this paper, however.

The results hold also if renegotiation is permitted. When renegotiation is possible, moral hazard problems are often expected to worsen (Fudenberg and Tirole, 1990). But Chung (1991) and Aghion et al. (1994) have shown how the initial contract can provide

cooperation and by Gatsios and Karp (1992) to show that firms may invest *more* if they anticipate future merger negotiations. When allowing negotiations on price, but not on investments, in a more general setting, Fershtman and Pakes (2000) use numerical analysis.

⁷For example, Hoel (1993) studies a differential game with an emission tax, Yanase (2006) derives the optimal contribution subsidy, Houba et al. (2000) analyze negotiations over (fish) quotas lasting forever, while Sorger (2006) studies one-period agreements. Although Ploeg and de Zeeuw (1992) even allow for R&D, contracts are complete or absent in all these papers.

incentives by affecting the bargaining position associated with particular investments.⁸ While these models have only one period, Guriev and Kvasov (2005) present a dynamic moral hazard problem emphasizing the termination time. Their contract is renegotiated at every point in time, to keep the remaining time horizon constant. Contribution levels are not negotiated, but contracting on time is quite similar to contracting on quantity, as studied by Edlin and Reichelstein (1996): to increase investments, Guriev and Kvasov let the contract length increase, while Edlin and Reichelstein let the contracted quantity increase. In this paper, agents can contract on quantity (of emissions) as well as on time, which permits the study of how the two interact. I also allow an arbitrary number of agents, in contrast to the buyer-seller situations in these papers.

3. The Model

3.1. Stocks and Preferences

This section presents a game where a set of $N \equiv \{1, \dots, n\}$ agents contribute over time to a public bad while they also invest in technology. The public bad is represented by the stock G . Allowing for a more or less long-lasting stock, let $1 - q_G \in [0, 1]$ measure the fraction of G that "depreciates" from one period to the next. The stock G may nevertheless increase, depending on the contribution or "emission" level g_i from agent $i \in N$:

$$G = q_G G_- + \sum_N g_i. \quad (3.1)$$

Parameter G_- represents the level of the public bad left from the previous period; subscripts for periods are thus skipped.

Each agent $i \in N$ benefits privately from emitting g_i . For example, if G measures the level of greenhouse gases, g_i is fossil-fuel consumption by country i . As an alternative to fossil fuel, i may consume renewable energy. Let the technology stock R_i measure how much energy i can produce using its renewable energy sources. Thus, R_i can be interpreted as the capacity of the "windmill park" in country i . The stock R_i might also

⁸Segal and Whinston (2002) generalize many related models.

depreciate over time, at the rate $1 - q_R \in [0, 1]$. Each "windmill" costs K units, and r_i measures how much i invests in its technology stock. Thus, if $R_{i,-}$ measures i 's technology stock in the previous period, its current technology is given by:

$$R_i = q_R R_{i,-} + r_i. \quad (3.2)$$

Since the technology can generate R_i units of energy, the total amount consumed by i is given by

$$y_i = g_i + R_i. \quad (3.3)$$

As an alternative interpretation, R_i may measure i 's "abatement technology," i.e., the amount by which i can at no cost reduce (or clean) its potential emissions. If energy production, measured by y_i , is otherwise polluting, the actual emission level of country i is given by $g_i = y_i - R_i$, which again implies equality (3.3). For either interpretation, i 's technology provides a private substitute to contributing to the public bad.

The investment stages and the pollution stages alternate over time. Define "a period" to be such that the countries first simultaneously invest in technology, after which they simultaneously decide how much to emit (see Figure 1).

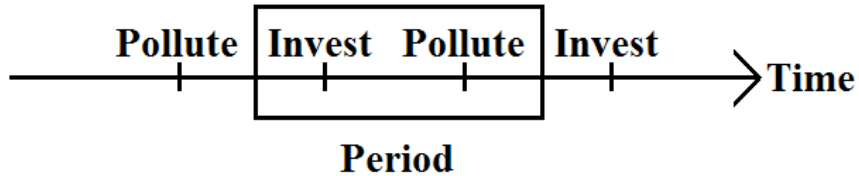


Figure 1: The definition of a period

Let the benefit of consumption be given by the increasing and concave function $B(y_i)$. If $C(G)$ is an increasing convex function representing each country's cost of the public bad, i 's utility in a period is:

$$u_i = B(y_i) - C(G) - Kr_i.$$

Country i 's objective is to maximize the present-discounted value of its future utilities,

$$U_{i,t} = \sum_{\tau=t}^{\infty} u_{i,\tau} \delta^{\tau-t},$$

where δ is the common discount factor and $U_{i,t}$ is i 's continuation value as measured at the start of period t . As mentioned, subscripts denoting period t are typically skipped when this is not confusing.

For alternative applications, one could interpret $-G$ as a public *good* and $-g_i$ as i 's contribution. The marginal benefit of the public good is then $C' > 0$, but the private marginal cost of contributing to the public good is $B'(R_i - (-g_i)) > 0$. Naturally, this marginal cost increases in the contribution level $-g_i$, but declines in the (cost-reducing) technology R_i . Sections 5 and 6 discuss how the model can be extended, and the results survive, if we allow for technological spillovers, uncertainty, and heterogeneity.

3.2. The Equilibrium Concept

As in most stochastic games, attention is restricted to Markov perfect equilibria (MPEs) where strategies are conditioned on the physical stocks only. As in Maskin and Tirole (2001), I look for the coarsest set of such strategies. Maskin and Tirole (2001: 192-3) defend MPEs since they are "often quite successful in eliminating or reducing a large multiplicity of equilibria," and they "prescribe the simplest form of behavior that is consistent with rationality" while capturing the fact that "bygones are bygones more completely than does the concept of subgame-perfect equilibrium." In this model, the MPE turns out to be unique and coinciding with the unique subgame-perfect equilibrium if time were finite and approaching infinity. This result is desirable; in fact, Fudenberg and Tirole (1991: 533) have suggested that "one might require infinite-horizon MPE to be limits of finite-horizon MPE."

If the agents are negotiating a contract, I assume the outcome is efficient and symmetric *if* the payoff-relevant variables are symmetric across agents. These assumptions are weak and satisfied in several situations. For example, we could rely on cooperative solution concepts, such as the Nash Bargaining Solution (with or without side transfers). Alternatively, consider a noncooperative bargaining game where one agent can make a take-it-or-leave-it offer to the others, and side transfers are feasible. If every agent has the same chance of being recognized as the proposal-maker, the equilibrium contract is exactly as described below.

All countries participate in the contract in equilibrium, since there is no stage at which they can commit to not negotiating with the others.

4. Analysis

For future reference, the first-best emission level g_i^* ex post (taking the stocks R_1, \dots, R_n and G_- as given) equalizes the private marginal benefit of consumption to the social cost of pollution:

$$B' = n(C' - \delta U_G) > 0, \text{ where} \quad (4.1)$$

$$B' \equiv \partial B(g_i^* + R_i) / \partial g_i, \quad C' \equiv \partial C(G) / \partial G, \quad U_G = -q_G(1 - \delta q_R) K / n.$$

Implicitly, the g_i^* s are functions of G_- and $\{R_1, \dots, R_n\}$. The first-best investment level equalizes the marginal benefit to the marginal cost, recognizing that more investments today reduce the need to invest in the next period:

$$B'(g_i + R_i^*) = (1 - \delta q_R) K. \quad (4.2)$$

By substituting (4.2) in (4.1), we find the first-best public bad level:

$$C'(G) = (1 - \delta q_G)(1 - \delta q_R) K. \quad (4.3)$$

Combined with (3.1), equation (4.3) pins down $\sum_N g_i$. Since (4.2) implies that y_i is the same across the i s, then, when investments are efficient, we can write the first-best emission level as:

$$\begin{aligned} g_i^{fb} &= \frac{1}{n} [C'^{-1}([1 - \delta q_G][1 - \delta q_R] K) - q_G G_- + R^*] - R_i^*, \text{ where} \\ R^* &\equiv \sum_N R_i^*. \end{aligned} \quad (4.4)$$

Given the g_i s, (4.2) determines the first-best R_i^* s which, with (3.2), determine the first-best r_i s. Throughout the analysis, I assume that $g_i \geq 0$ and $r_i \geq 0$ never bind.⁹

⁹In every equilibrium considered below, $g_i > 0$ and $r_i > 0$ always hold. Thus, it can be verified in retrospect that the constraints will never bind.

4.1. The Noncooperative Outcome

In principle, the continuation value U_i is a function of the $n+1$ stocks G_- and $\{R_1, \dots, R_n\}$. However, note that choosing g_i is equivalent to choosing y_i , once the R_i s are sunk. Substituting (3.3) into (3.1), we get:

$$G = q_G G_- + \sum_N y_i - R. \quad (4.5)$$

This way, the R_i s are eliminated from the model: they are *payoff-irrelevant* as long as $R \equiv \sum_N R_i$ is given, and i 's Markov perfect strategy for y_i is thus not conditioned on them.¹⁰ A country's continuation value U_i is thus a function of G_- and R_- , not $R_{i,-} - R_{j,-}$, and we can therefore write it as $U(G_-, R_-)$, without the subscript i .

Because of the linear investment cost, it turns out that the continuation value U must be linear in *both* payoff-relevant stocks, even though u_i is nonlinear in G . This linearity makes the model tractable and simple to work with. Furthermore, the linearity permits only one equilibrium.

PROPOSITION 1. Equilibrium properties:

- (i) *There is a unique symmetric MPE.*
- (ii) *The equilibrium is in stationary strategies.*
- (iii) *The continuation value $U_i(G, R_1, \dots, R_n) = U(G, R)$ is linear in the stocks, with:*

$$\begin{aligned} U_R &= q_R K/n \text{ and} \\ U_G &= -q_G (1 - \delta q_R) K/n. \end{aligned} \quad (4.6)$$

Proposition 1, along with the other results, is proven in the appendix.¹¹ The rest of this section describes the equilibrium in more detail.

¹⁰This follows from the definition by Maskin and Tirole (2001, p. 202), where Markov strategies are measurable with respect to the coarsest partition of histories consistent with rationality.

¹¹As the proposition states, this is the unique *symmetric* MPE. Since the investment cost is linear, there also exist asymmetric MPEs in which the countries invest different amounts. Asymmetric equilibria may not be reasonable when countries are homogeneous, and they would cease to exist if the investment cost were convex.

At the emission stage, when the technologies are sunk, i solves

$$\begin{aligned} \max_{y_i} B(y_i) - C(G) + \delta U(G, R) \text{ s.t. } (4.5) &\Rightarrow \\ B'(y_i) = C' - \delta U_G. & \end{aligned} \quad (4.7)$$

First, note that each country pollutes too much compared to the first best (4.1). The marginal benefit of polluting, $B'(g_i + R_i)$, decreases in g_i and it can be interpreted as the shadow value of polluting one more unit, fixing the total level of emission. Thus, B' would be the equilibrium permit price if the emission quotas were tradable across the countries (allowing for such trade would not alter the results). In the noncooperative equilibrium, each country limits its emission (since $B' > 0$), but it internalizes only $1/n$ of the total harm.

Second, (4.7) verifies that each i chooses the same y_i , no matter the R_i s. While perhaps surprising at first, the intuition is straightforward. Every country has the same preference for (and marginal benefit from) consuming y_i , and the *marginal* cost, through G , is also the same for every country: one *additional* consumed unit generates one unit of public bad.¹²

Substituting (4.5) in (4.7) implies that a larger R must increase every y_i . This implies that if R_i increases but R_j , $j \neq i$, is constant, then $g_j = y_j - R_j$ must increase. Furthermore, substituting (3.3) in (4.7) implies that if R_i increases, g_i must decrease. In sum, if country i has better technology, i pollutes less but (because of this) other countries pollute more. In addition, in the next period all countries invest less. Clearly, these effects discourage countries from investing.

PROPOSITION 2. Investments:

(i) *Even if past investments differed, every $i \in N$ consumes the same:*

$$y_i^{no} = y_j^{no} \quad \forall i, j \in \{1, \dots, n\} \forall R_i, R_j. \quad (4.8)$$

(ii) *If i invests more, i pollutes less but $j \neq i$ pollutes more, and everyone invests less the*

¹²This follows from (3.3), and would not necessarily be true if I instead had focused on technologies that reduced the emission *content* of *each* produced unit (e.g., $g_i = y_i/R_i$). The additive form (3.3) is chosen - not only because it simplifies the analysis tremendously - but also because the resulting crowding-out effects might be reasonable in reality.

following period:

$$\partial g_i^{no} / \partial R_i = -\frac{C'''(n-1) - B''}{nC''' - B''} < 0, \quad (4.9)$$

$$\partial g_i^{no} / \partial R_j = \frac{C'''}{nC''' - B''} > 0 \quad \forall j \neq i, \quad (4.10)$$

$$\partial r_i^{no} / \partial R_- = -q_R/n. \quad (4.11)$$

(iii) *Consequently, investments are too low, compared to the first best.*

Results (i)-(ii) mean that a country's technology stock is, in effect, a public good. A larger R_i raises every country's consumption and reduces every investment in the following period. Since i captures only $1/n$ of the benefits, i invests less than optimally.

At the emission stage, as already noted, a country consumes too much since it does not take into account the harm imposed on the other countries. In addition, the appendix shows that, in equilibrium, r_i increases in G_- . Anticipating this, a country may want to pollute a lot in order to induce the other countries to invest more in the next period.¹³

PROPOSITION 3. Emissions and consumption:

(i) *If i pollutes more, every $j \in N$ invests more in the following period:*

$$\partial r_i^{no} / \partial G_- = q_G/n. \quad (4.12)$$

(ii) *Emission levels are too large compared to the first best.*

(iii) *Nevertheless, the equilibrium consumption level y_i is lower than it would be in the first best.*

Part (iii) states that the reduction in r_i always dominates the increase in g_i , such that the consumption level $y_i = g_i + R_i$ is always less in the noncooperative equilibrium than the first-best level of y_i . With these dynamic effects, this common-pool problem is more severe than its static counterpart (or than the open-loop equilibrium).¹⁴

¹³Adding to the public good $-G$ (by reducing g_i) or to R (by increasing r_i) has somewhat similar effects. However, they are not equivalent since a larger r_i reduces emissions in *every* future period. Increasing r_i thus has a longer-lasting impact than reducing g_i , which is why r_i is referred to as an investment. Moreover, the next sections let g_i be contractible but not r_i .

¹⁴This is also the case in Ploeg and de Zeeuw (1991), for example, and it is verified in experiments by Battaglini et al. (2010).

4.2. Negotiations and Incomplete Contracts

From now on, I let the countries negotiate and contract on their contributions to the public bad. Whether a country i complies by reducing its current consumption or by investing in a more long-term solution is up to country i . The other countries may, in any case, find it hard to verify which course was chosen.

The model can (and will) be used to analyze agreements of any length. In this subsection, countries negotiate and contract in the beginning of each period. Thus, the period length is defined by the contract length. Obviously, each period and contract can be arbitrarily long, since I have not specified the level of the discount factor, for example.

In each period, the timing is the following. First, the countries negotiate a vector of contribution levels g_i . Thereafter, each country sets r_i and, finally, every country complies with the contract. As mentioned, I assume the bargaining outcome is efficient and symmetric *if* the game itself is symmetric. If negotiations fail, the countries play noncooperatively.

The bargaining game is indeed symmetric, even if $R_{i,-}$ differs across the countries. Just as in Section 4.1, the $R_{i,-}$ s are eliminated from the model and the continuation value is a function of only G_- and $R_- \equiv \sum_N R_{i,-}$. Moreover, the linear investment cost implies that U must be linear in both stocks, pinning down a unique equilibrium. In fact, the equilibrium properties simplifying the analysis above continue to hold with incomplete contracts. In particular, there is a unique MPE and the continuation value is linear, with the same slopes as before.

PROPOSITION 4. Equilibrium properties (Proposition 1 continues to hold):

- (i) *There is a unique MPE.*
- (ii) *The equilibrium is in stationary strategies.*
- (iii) *The continuation value $U_i(G, R_1, \dots, R_n) = U(G, R)$ is linear in the stocks, with:*

$$\begin{aligned} U_R &= q_R K/n \text{ and} \\ U_G &= -q_G (1 - \delta q_R) K/n. \end{aligned}$$

When investing, $i \in N$ prefers a larger stock of technology if its quota, g_i^{co} , is small, since otherwise its consumption level would be very low. Consequently, r_i decreases in g_i^{co} . For a given g_i^{co} , the investment level r_i increases until R_i satisfies:

$$B'(g_i^{co} + R_i^{co}) = K - \delta U_R = K(1 - \delta q_R/n). \quad (4.13)$$

In contrast to the noncooperative game, R_i is no longer a public good: once the emission levels are pinned down, i 's investment increases y_i but not y_j , $j \neq i$. However, the technology that survives to the next period, $q_R R_i$, does become a public good, since, for a fixed R , the continuation value at the start of every period is independent of R_i . Intuitively, if the agreement does not last forever, a country anticipates that good technology will worsen its bargaining position in the future, once a new agreement is to be negotiated. At that stage, good technology leads to a lower $g_{i,+}$ since the other countries can hold i up when it is cheap for i to reduce its emissions.¹⁵ In fact, $y_{i,+}$ is going to be the same across the i s, no matter what the differences are in the R_i s. This discourages i from investing now, particularly if the current agreement is relatively short (δ large), the technology likely to survive (q_R large), and the number of countries n large. Thus, compared to the first best (4.2), countries still underinvest if $\delta q_R > 0$.

PROPOSITION 5. Investments:

- (i) *Country $i \in N$ invests more if the contract is tough: $\partial r_i / \partial g_i^{co} = -1$.*
- (ii) *Nevertheless, for any given g_i^{co} , i underinvests if the agreement is relatively short-lasting ($\delta > 0$) while the technology long-lasting ($q_R > 0$).*

Thus, if δ and q_R are large, it is important to encourage more investments. On the one hand, this can be achieved by a small g_i^{co} . On the other, the ex-post optimal g_i^{co} is larger when equilibrium investments are low. The optimal g_i^{co} s must trade off these concerns. As shown in the appendix, the equilibrium and optimal g_i^{co} s must satisfy (4.4): the equilibrium quotas are identical to the first-best levels!¹⁶

¹⁵Or, if no agreement is expected in the future, a large $R_{i,+}$ reduces $g_{i,+}$ and increases $g_{j,+}$, as proven in Section 4.1.

¹⁶Technically, the reason is that y_i is in equilibrium independent of g_i^{co} , since $\partial R_i / \partial g_i^{co} = -1$. Thus, the marginal costs and benefits of increasing g_i^{co} have the same levels as in the first-best scenario, in which the effect on y_i can be ignored using the envelope theorem.

However, since (4.13) implies that the equilibrium R_i^{co} s are less than optimal, the g_i^{lt} s are suboptimally low *ex post*. Combining (4.3) and (4.13) gives

$$B' = n(C' - \delta U_G) + (1 - 1/n) K \delta q_R. \quad (4.14)$$

Not only is the shadow value of polluting, B' , larger than in the noncooperative case, but it is even larger than it would be in the first best, (4.1). For a fixed investment level, optimally g_i^{co} should have satisfied $B' = n(C' - \delta U_G)$ rather than (4.14). Only then would marginal costs and benefits be equalized. Relative to this *ex-post* optimal level, the g_i^{co} satisfying (4.14) must be *lower* since $B' - n(C' - \delta U_G)$ decreases in g_i^{co} . If n , q_R , and δ are large, the additional term $(1 - 1/n) K \delta q_R$ is large, and g_i^{co} must decline. This makes the contract more demanding or *tougher* to satisfy at the emission stage, compared to what is *ex post* optimal. The purpose of committing to such an overambitious agreement is to encourage investments, since these are suboptimally low when n , q_R , and δ are large.

PROPOSITION 6. The equilibrium contract:

- (i) *The contracted emission levels are equal to the levels at the first best (4.4).*
- (ii) *But the emission levels are lower than what is ex post optimal (4.1) if the agreement is short-term ($\delta > 0$) while the technology is long-lasting ($q_R > 0$).*

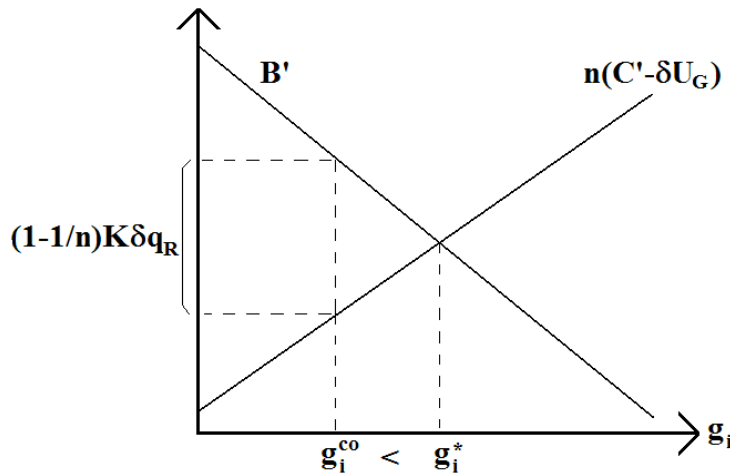


Figure 2: The shorter the agreement, the lower is the contracted emission level relative to the *ex post* optimum

Figure 2 illustrates the main result: if the length of the agreement is relatively short, δ and q_R are large, and the quotas should be much smaller relative to the emission levels that are ex post optimal. For example, suppose $B(y_i) = -b(\bar{y} - y_i)^2/2$ and $C(G) = cG^2/2$. If g_i^* measures the ex-post optimal pollution level, conditioned on equilibrium investment levels, then:

$$g_i^{co} = g_i^* - \frac{\delta q_R K (1 - 1/n)}{b + cn^2}.$$

On the other hand, if $\delta q_R = 0$, the right-hand side of (4.14) is zero, meaning that the commitments under the best long-term agreement also maximize the expected utility ex post. In this case, the countries are not concerned with how current technologies affect future bargaining power, either because the existing agreement is lasting forever ($\delta = 0$), or because the technology will not survive the length of the contract ($q_R = 0$). Investments are first best and there is no need to distort the g_i^{co} s downwards.

4.3. Multiperiod Contracts

Assume now that at the beginning of period 1, the countries negotiate the $g_{i,t}$ s for every period $t \in \{1, 2, \dots, T\}$. The time horizon T may be limited by the countries' ability to commit to future promises.

Just as before, the payoff-relevant stocks at the start of period 1 are G_- and R_- only. Once again, this simplifies the analysis. There is a unique MPE, the continuation value at the start of period 1 (and $T + 1$) is linear in the stocks, and has the same slopes as before.

PROPOSITION 7. Equilibrium properties (Proposition 1 continues to hold):

- (i) *There is a unique MPE.*
- (ii) *The equilibrium is in stationary strategies.*
- (iii) *The continuation value $U_i(G, R_1, \dots, R_n) = U(G, R)$ is linear in the stocks, with:*

$$\begin{aligned} U_R &= q_R K/n \text{ and} \\ U_G &= -q_G (1 - \delta q_R) K/n. \end{aligned}$$

When investing in period $t \in \{1, 2, \dots, T\}$, countries take the $g_{i,t}$ s as given, and the continuation value in period $T + 1$ is $U(G_T, R_T)$. At the last investment stage, i 's problem

is the same as in Section 3.2 and i invests until (4.13) holds. Anticipating this, i can invest less in period T by investing more in period $T - 1$. The net investment cost is thus $K(1 - \delta q_R)$. The same logic applies to every previous period and, in equilibrium,

$$B'(g_{i,t} + R_{i,t}) = K(1 - \delta q_R) \text{ for } t < T. \quad (4.15)$$

Thus, the incentives to invest are larger earlier than in the last period, given by (4.13). In fact, investments are equal to the first best (4.2) for every $t < T$.¹⁷

PROPOSITION 8. Investments:

- (i) *Investments decrease toward the end of the agreement.*
- (ii) *They are socially optimal for $t < T$, but suboptimally low in the last period.*

Intuitively, the countries invest less when future negotiations are coming up because of the hold-up problem, but they invest more (and optimally) if the emission levels are pinned down for the next period as well. All this is anticipated when the countries negotiate the $g_{i,t}$ s.

As shown in the appendix, the optimal and equilibrium $g_{i,t}$ s must satisfy (4.3) for every $t \leq T$: the equilibrium pollution level is similar to the first-best level, for every period!

In the beginning of the agreement, when $t < T$, the $g_{i,t}$ s are *ex post* optimal as well, since the investments are first best. In the last period, however, investments decline and the contracted emission levels are lower than the ex-post optimal levels. In other words, the optimal contract becomes tougher to satisfy toward its end (and the shadow value of polluting, or the permit price, B' , increases).

PROPOSITION 9. The equilibrium contract:

¹⁷Since $R_T < R_{T-1}$, investments may be negative in period T . The condition for when investments are always positive is:

$$\begin{aligned} \sum_N r_i &= R_T - q_R R_{T-1} = B'^{-1}(K(1 - \delta q_R/n)) - g_{i,T}^{co} - q_R B'^{-1}(K(1 - \delta q_R)) + g_{i,T-1}^{co} \\ &= B'^{-1}(K(1 - \delta q_R/n)) - q_R B'^{-1}(K(1 - \delta q_R)) \\ &\quad - (1 - q_R)(1 - q_G) \frac{1}{n} C'^{-1}[(1 - \delta q_G)(1 - \delta q_R)K] > 0. \end{aligned}$$

- (i) For every period, the contracted emission levels equal the first-best levels (4.4).
- (ii) Since investments are suboptimally low in the last period, the contract becomes tougher to satisfy toward the end, and emission levels are then too low, relative to the ex post optimum (4.1), if $\delta q_R > 0$.

4.4. Renegotiation

The contracts above are not renegotiation-proof, since they specify emission levels that are less than what is optimal ex post, after the investments are sunk. The countries may thus be tempted to renegotiate the treaty. This section derives equilibria when renegotiation is costless.

Starting with one-period contracts, the timing in each period is the following. First, the countries negotiate the initial commitments, the g_i^{de} s, referred to as "the default." If these negotiations fail, it is natural to assume that the threat point is no agreement.¹⁸ Thereafter, the countries invest. Before carrying out their commitments, the countries get together and renegotiate the g_i^{de} s. Relative to the threat point g_i^{de} , the bargaining surplus is assumed to be split equally in expectation. As before, this bargaining outcome is implemented by, for example, randomly letting one country make a take-it-or-leave-it offer regarding quantities and transfers.

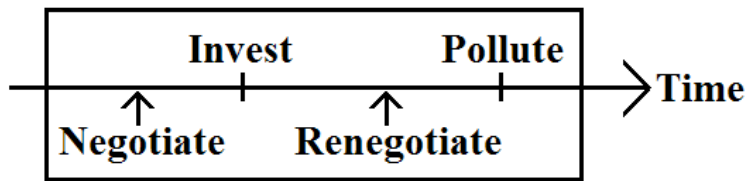


Figure 3: The timing when renegotiation is possible

At the start of each period, any difference in technology is payoff-irrelevant and the continuation value is a function of G_- and R_- only, just as before. Moreover, this continuation value is linear in the stocks, leading to a unique equilibrium. For this game also, the earlier appealing equilibrium properties continue to hold.

¹⁸However, if the threat point were "short-term" agreements, negotiated after the investment stage, the outcome would be identical.

PROPOSITION 10. Equilibrium properties (Proposition 1 continues to hold):

- (i) *There is a unique MPE.*
- (ii) *The equilibrium is in stationary strategies.*
- (iii) *The continuation value $U_i(G, R_1, \dots, R_n) = U(G, R)$ is linear in the stocks, with:*

$$\begin{aligned} U_R &= q_R K/n \text{ and} \\ U_G &= -q_G (1 - \delta q_R) K/n. \end{aligned}$$

Renegotiation ensures that emission levels are ex post optimal, in contrast to the contracts discussed above. When investing, a country anticipates that it will not, in the end, have to comply with an overambitious contract. Will this jeopardize the incentives to invest?

Not necessarily. When renegotiating an *ambitious* agreement, countries that have invested little are desperate to reach a new agreement that would replace the tough initial commitments. Such countries have a poor bargaining position, and so they will, in equilibrium, compensate the others for relaxing the quotas. Fearing this, all countries are induced to invest more, particularly if the default emission levels are small.

PROPOSITION 11. Investments:

Country i 's investment level r_i decreases in the initial quota g_i^{de} .

This is anticipated when negotiating the initial agreement, the g_i^{de} s. The more ambitious this agreement is, the more the countries invest. This is desirable if the countries are otherwise tempted to underinvest. Thus, the agreement should be more ambitious if δ and q_R are large. Since the investments are influenced by the initial agreement, the g_i^{de} s can always be set such that the investments are first best. In any case, the emission levels remain optimal, thanks to renegotiation. In sum, the optimal and equilibrium contract implements the first best.

PROPOSITION 12. The equilibrium contract:

- (i) *The initial contract satisfies (4.16), and it is thus tougher if it is relatively short-term (δ large) while the technology is long-lasting (q_R large).*

(ii) *In equilibrium, all investments and emissions are first best.*

$$B'(g_i^{de} + R_i^*) = K \Rightarrow \quad (4.16)$$

$$g_i^{de} = g_i^* - [B'^{-1}(K[1 - \delta q_R]) - B'^{-1}(K)] < g_i^*.$$

To see the second part of (i), note that (4.16) requires that g_i^{de} decreases in δq_R since R_i^* is increasing in δq_R . Intuitively, if the length of the agreement is short, countries fear that more technology today will hurt their bargaining position in the near future. They thus invest less than what is optimal, unless the agreement is more ambitious.

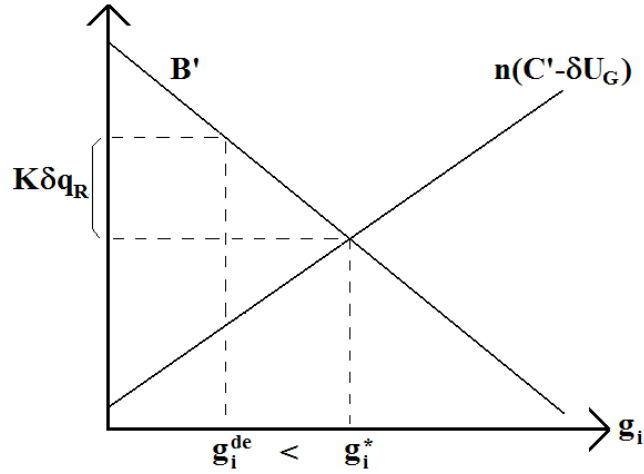


Figure 4: *The shorter the agreement, the lower is the contracted emission level relative to the ex post optimum*

This result is illustrated in Figure 4, and it confirms the comparative static for the case without renegotiation (Proposition 6).

Compared to the optimal contract without renegotiation, given by (4.14), the initial agreement should be tougher when renegotiation is possible ($g_i^{de} < g_i^{co}$). Intuitively, without renegotiation the contract balances the concern for investments (by reducing g_i^{co}) and for ex-post efficiency (where g_i should be larger). The latter concern is irrelevant when renegotiation ensures ex-post optimality, so the initial contract can be tougher - indeed, so tough that investments are first best.

COROLLARY 1. *The initial contract under renegotiation (4.16) is tougher and specifies lower emission levels than the equilibrium contract when renegotiation is not possible (4.14).*

Implementation:

Note that the equilibrium outcome is observationally equivalent to a time-inconsistency problem where the countries make ambitious plans for the future, while repeatedly backing down from promises made in the past. But rather than reflecting a time-inconsistency problem, this actually leads to the first best.

COROLLARY 2. In equilibrium, the countries repeatedly promise to pollute little in the future but when the future arrives, they renege on these promises. This procedure implements the first best.

Multiple periods:

If the countries can negotiate and commit to a T -period agreement, we know from Section 4.3 that investments (and consumption) are first best in every period - except for the last. Thus, the contracted quantities are also ex-post optimal, and there is no need to renegotiate them. It is only in the last period that the quantities are lower than what is optimal ex post, and only then is there an incentive to renegotiate the contract. When the countries anticipate that the contract will be renegotiated in the last period, they do not need to trade off the concern for ex-post efficiency for the need to encourage investments, and the initial contract can be tougher, and in fact so tough that investments are first best, even in the last period.

Thus, when renegotiation is possible, for every period but the last the optimal and equilibrium initial contract specifies the ex-post optimal quantities, and these are also equal to the first-best quantities since investments are optimal for $t < T$. The initial contract for the last period, $t = T$, is given by (4.16), just as in the one-period contract with renegotiation. As before, the initial contract becomes tougher to satisfy towards its end, since the initial quotas are smaller in the last period than in the earlier periods.¹⁹

PROPOSITION 13. Multiple periods and renegotiation:

¹⁹To see this, note that the last-period contract (4.16) can be compared to the earlier (first-best) quantities by writing the latter as

$$B'(g_{i,t}^{de} + R_i^*) = K(1 - \delta q_R).$$

- (i) For $t < T$, the equilibrium initial contract is given by $g_{i,t}^{de} = g_i^*$ but for $t = T$, the contract is tougher and given by (4.16).
- (ii) This contract is renegotiated only after the investment stage in the last period.
- (iii) The first best is implemented by any T -period contract, $T \geq 1$, when renegotiation is possible.

5. Technological Spillovers

In the benchmark case above, investments were selfish. For some applications, however, it might be reasonable that i benefits from j 's investments. Coe and Helpman (1995) find that technological spillovers are empirically important, and they let spillovers have an additive impact. Thus, if a larger r_i increases R_i directly by d units, suppose R_j increases by e units, $\forall j \in N \setminus i$. Parameter $e \geq 0$ measures the technological spillover. The total impact of r_i on R is $D \equiv d + e(n - 1)$, and we can write:

$$R_i = q_R R_{i,-} + (D - e(n - 1)) r_i + \sum_{j \in N \setminus i} e r_j.$$

The appendix solves the model for any e .

In the noncooperative case, the level of e turns out to be irrelevant for investments as well as for consumption. The reason is that R_i is, in any case, a perfect public good, no matter the level of e .

Suppose, next, that countries negotiate emission levels but that renegotiation is not possible. Once the emission levels are pinned down, then a positive e implies that j can consume more if i invests. This externality is a second reason that i invests suboptimally little - in addition to the hold-up problem emphasized so far. The larger e is, the lower the investment levels are, compared to the first-best level. The reduction in investments implies that it is ex post optimal to pollute more. On the other hand, by negotiating smaller emission levels, the countries invest more, and this is beneficial for everyone when the countries invest suboptimally little because of $e > 0$. Balancing these concerns, it turns out that the optimal G and g_i are independent of e , given D . In any case, the equilibrium contract specifies the emission levels given by (4.3)-(4.4), as would have been first best if investments had been efficient.

But since investments are suboptimally low, the negotiated g_i s are lower than what is ex post optimal. In the one-period contract analyzed in Section 4.2, the appendix shows that the contracted quotas will satisfy:

$$B' - n(C' - \delta U_G) = \frac{K}{D} \left(\frac{e(1 - \delta q_R)(n - 1) + \delta q_R(1 - 1/n)}{D - e(n - 1)} \right). \quad (5.1)$$

After the investments are sunk, it would be (ex-post) optimal to pollute more and so much that the left-hand side were equal to zero. Compared to this ex-post optimal level, the agreement should be tougher and more ambitious when e is large. For multiperiod contracts, (5.1) would be satisfied for the last period, when $t = T$. For the earlier periods, $t < T$, the optimal and equilibrium quotas will satisfy:

$$B' - n(C' - \delta U_G) = \frac{K}{D} \left(\frac{e(n - 1)(1 - \delta q_R)}{D - e(n - 1)} \right). \quad (5.2)$$

Thus, when the spillover is positive, the optimal agreement is "overambitious" for every period, not only the last.

When renegotiation is possible, the first best is still obtainable by the appropriate initial contract if just $e < D/n$. For one-period contracts, this initial contract should satisfy:

$$B'(g_i^{de} + R_i^*) = \frac{K}{D - en}. \quad (5.3)$$

For multiperiod contracts, when $t < T$, the first best is implemented if:

$$B'(g_{i,t}^{de} + R_i^*) = \frac{K(1 - \delta q_R)}{D - en}. \quad (5.4)$$

To achieve the first best, note that even the multiperiod contract must be renegotiated in every period when $e > 0$. In that case, a multiperiod contract is overambitious in order to motivate R&D, and for every period it specifies emission levels that are lower than those that are optimal once the investments are sunk. While this encourages investments, it also necessitates renegotiation.

To summarize, for all these cases, a larger spillover implies that the contract should be tougher relative to the level that is ex-post optimal.²⁰

²⁰For the one-period contract, this finding is also detected by Golombek and Hoel (2005). When renegotiation is possible, a related result is derived for the buyer-seller game in Edlin and Reichelstein (1996). If $e \geq d$, however, the first best can never be implemented, a finding which is in line with Che and Hausch (1999). However, all these contributions limit their attention to one-period models.

PROPOSITION 14. *The larger is the technological spillover e , the tougher is the optimal and equilibrium contract relative to the ex post optimum. The T -period contract is given by:*

- (i) *condition (5.1) for $t = T$ if renegotiation is impossible;*
- (ii) *condition (5.2) for $t < T$ if $T > 1$ and renegotiation is impossible;*
- (iii) *condition (5.3) for $t = T$ if renegotiation is possible;*
- (iv) *condition (5.4) for $t < T$ if $T > 1$ and renegotiation is possible.*

6. Generalizations and Extensions

One purpose of this paper is to present a model that is simple and tractable, despite the complexity of the underlying problem. The results are robust to several generalizations, and the model can fruitfully be expanded in various directions. This section briefly describes some of these extensions.

6.1. Robustness to the Future Regime

When analyzing a particular game, I have so far assumed that the identical game repeats itself after one period or contract has expired. Obviously, the equilibrium in a given period is a function of the future continuation-value function. However, while the derivatives U_R and U_G determine the incentives to invest and to pollute, the *level* of U is irrelevant for these choices. For all the regimes analyzed above, it turned out that U_R and U_G were constant and identical: Proposition 1 continued to hold throughout the analysis. Thus, the equilibrium for a given period or contract is unchanged if, in the next period, the countries play noncooperatively or instead negotiate a contract (of any length, with or without renegotiation).

COROLLARY 3. *For each period, every equilibrium derived above remains unchanged whether the countries in the next (or any future) period (i) act noncooperatively, (ii) negotiate one-period contracts, (iii) negotiate multiperiod contracts, or (iv) negotiate default contracts that will be renegotiated later.*

6.2. Adding Uncertainty

While the model above is deterministic, certain types of uncertainty leave the results unchanged. Since the continuation values are linear in R , countries are risk-neutral in that it would not matter if, say, the depreciation rate on technology were random, as long as the *expected* depreciation rate is $1 - q_R$. The realized depreciation can also be different for every country, as long as the expected depreciation rate is $1 - q_R$ for everyone. In addition, the cost of pollution at time t may depend on some state θ_t such that it could be written $C(G_t, \theta_t)$. Again, Propositions 1-14 continue to hold if one simply replaces C' in every expression by the *expected* marginal cost, EC' , where the expectations are taken with respect to the unknown future θ_t . Since $C(\cdot)$ is strictly convex, $EC'(G_t, \theta_t) > C'(G_t, E\theta_t)$, and G_t should thus be smaller when θ_t is uncertain. One can thus expect that, for a T -period agreement, the optimal $g_{i,t}$ s should decrease in t due to the (increased) uncertainty in θ_t . This strengthens the conclusion that a long-term agreement should become tougher to satisfy over time.

6.3. Endogenizing the Contract Length

Above, I have taken the contract's length, T , to be exogenous. This may be reasonable if T measures the length of time to which the countries can commit. If the countries could choose, they would always prefer T to be as large as possible.

This would no longer be true, however, if uncertainty were added to the model. If θ_t in $C(G_t, \theta_t)$ is stochastic, for example, there is a cost of committing in advance to future emission levels, if these cannot be renegotiated or conditioned on θ_t . In this case, the optimal time horizon may be finite.

Alternatively, one may assume that there is a fixed cost of negotiating every period's emission levels. Since the cost of the hold-up problem is realized only in period T , the present discounted value of this cost is smaller than the fixed negotiation cost if T is large. Thus, such negotiation costs would imply that the optimal T is interior.

Whether T is pinned down by the uncertainty or by the negotiation cost, some comparative static is feasible. For example, if the technology is long-lasting (q_R is large), the

hold-up problem in period T is severe and, to delay this cost, the countries may prefer to increase T . In Harstad (2010), I allow for uncertainty and show how the optimal T depends on several parameters.

6.4. Heterogeneity

To provide a benchmark case, it has been assumed that the countries are completely symmetric and there has been no heterogeneity. It did turn out, however, that for a given R_- , differences in $R_{i,-}$ (such as $R_{i,-} - R_{j,-}$) were payoff-irrelevant. It is therefore not necessary to assume that all countries start out with the same technology.

Furthermore, some heterogeneity can easily be added to the model. For example, if country i 's benefit of consumption is measured relative to some individual bliss point or reference point \bar{y}_i , we could write i 's benefit as $B(y_i - \bar{y}_i)$. If we define $\tilde{y}_i \equiv y_i - \bar{y}_i$, every result above holds if y_i is substituted by \tilde{y}_i . While countries with large \bar{y}_i are going to consume more in every equilibrium, i 's consumption *relative* to its reference point is going to be constant across the countries.

6.5. Contractible Investments

If the countries negotiated investments but not emission levels, then deriving the best incomplete contract would require an analysis somewhat similar to that above. If both investments and emission levels were contractible, the first best could be implemented trivially, even without renegotiation. One way of implementing the first best is then to subsidize investments across countries. Without subsidies, investments are suboptimally low, particularly if the technology is long-lasting and the contract short-lasting or close to its expiration date. To ensure optimal investments, the subsidy should thus be larger for contracts that have a short time horizon and when they are close to expiring (for details, see Harstad, 2010).

6.6. Participation

In this paper, I have assumed that the agents cannot hide when negotiating a contract. Dixit and Olson (2000), on the other hand, study a two-stage game in which the agents first decide whether to participate in the second cooperative stage. With such a possibility of opting out, many agents prefer to abstain and free-ride. Thus, one might expect less than full participation in the present model as well, if such a stage were added to the model. However, in contrast to Dixit and Olson, the present game has several periods. Thus, if only a few agents decide to participate, they may prefer to contract for fewer periods, hoping that the nonparticipants will turn up later. Since short-term contracts lead to suboptimal investments, this (credible!) threat may discourage agents from considering to free-ride. Thus, participation may be larger than in the two-stage model of Dixit and Olson. Future research should investigate this conjecture - along with many other possible extensions.

7. Conclusions

This paper presents a novel dynamic game in which n agents contribute to a public bad while also investing in substitute technologies. Under the assumption of linear investment costs, the Markov perfect equilibrium (MPE) is unique, the continuation value linear, and the analysis tractable, despite the $n + 1$ stocks. While the unique equilibrium rules out self-enforcing agreements, the framework can be employed to analyze incomplete contracts in a dynamic setting.

With only one period, or if the contract lasted forever, contracting on contribution levels would be first best since investments are "selfish" in (most of) the paper. If the agents cannot commit to the end of time, however, investments are suboptimally low, particularly if the contract is short-term or close to expiring. To further motivate investments, the equilibrium and optimal contract is tougher and more ambitious if it is short-lasting or close to the expiration date. If renegotiation is possible, such a contract implements the first best.

While the model and the method are general, the assumptions fit well to the context

of climate change, and the results have important consequences for how to design a treaty. First, *even if* the countries can credibly commit to emission levels, they will invest too little in renewable energy sources and abatement technology. As a consequence, the climate treaty should be more ambitious compared to what is optimal ex post, after the investments are sunk. In particular, short-term agreements should be more ambitious than long-term agreements, and the agreement should be tougher towards the end.

Currently, the commitments made under the Kyoto Protocol expire in 2012 and the threat point for present negotiations is no agreement at all. This reduces the incentive to invest in new technologies, according to the above results. When the Doha-round trade negotiations broke down, on the other hand, the default outcome was *not* the noncooperative equilibrium but the existing set of long-term trade agreements. Long-lasting agreements permitting renegotiation can implement the first best in the above model. Thus, the procedure used for negotiating trade agreements is more efficient than the one currently used for climate, according to this analysis.

With this application, the paper provides a small step toward a better understanding of how climate treaties interact with the incentives to invest in technologies. The analysis has detected and explored challenges that arise *even if* we abstract from domestic politics, heterogeneity across countries, private information, monitoring, compliance, coalition formation, and the possibility of opting out of the agreement. While the effects discussed in this paper are likely to persist, allowing for such complications will certainly generate several new results and thereby enhance our understanding of the best agreement design. Relaxing these assumptions is thus the natural next step.

8. Appendix

All propositions are here proven allowing for technological spillovers. In Sections 3 and 4, $e = 0$ and $D = d = 1$.

While U_i is the continuation value just before the investment stage, let W_i represent the (interim) continuation value at (or just before) the emission stage. To shorten equations, use $m \equiv -\delta \partial U_i / \partial G_-$, $z \equiv \delta \partial U_i / \partial R_-$, $\tilde{R} \equiv q_R R_-$ and $\tilde{G} \equiv q_G G_-$. The proof for the first best (4.1)-(4.3) is omitted since it would follow the same lines as the following proof.

Proofs of Proposition 1-3.

Note that, by substitution,

$$\begin{aligned} G &= q_g G_- + \sum_N y_i - R, \text{ and} \\ u_i &= B(y_i) - C(G) - K r_i. \end{aligned}$$

Thus, all i 's are identical w.r.t. y_i and differences in the technology stock do not matter. The game is thus symmetric at the emission stage, no matter differences in R_i . At the investment stage, the game is symmetric, no matter differences in $R_{i,-}$. Analyzing the symmetric equilibrium (where symmetric countries invest identical amounts), I drop the subscript for i on U and W .

At the emission stage, each country's first-order condition for y_i is:

$$\begin{aligned} 0 &= B'(y_i) - C'(G) + \delta U_G(G, R) \\ &= B'(y_i) - C' \left(\tilde{G} - R + \sum_N y_i \right) + \delta U_G(\tilde{G} - R + \sum_N y_i, R), \end{aligned} \quad (8.1)$$

implying that all y_i s are identical and implicit functions of \tilde{G} and R only. At the investment stage, i maximizes:

$$W(\tilde{G}, R) - K r_i = W \left(q_G G_-, \tilde{R} + \sum_i D r_i \right) - K r_i, \quad (8.2)$$

implying that R is going to be a function of G_- , given implicitly by $\partial W(q_G G_-, R) / \partial R = K/D$ and explicitly by, say, $R(G_-)$. In the symmetric equilibrium, each country invests

$(R(G_-) - q_R R_-) / Dn$. Thus:

$$\begin{aligned} U(G_-, R_-) &= W(q_G G_-, R(G_-)) - K \left(\frac{R(G_-) - q_R R_-}{Dn} \right) \Rightarrow \\ z/\delta &\equiv \frac{\partial U}{\partial R_-} = \frac{q_R K}{Dn} \end{aligned} \quad (8.3)$$

in every period. Hence, $U_{RG} = U_{GR} = 0$, m and U_G cannot be functions of R and (8.1) implies that y_i , G and thus $B(y_i) - C(G) \equiv \gamma(\cdot)$ are functions of $\tilde{G} - R$ only. Hence, write $G(\tilde{G} - R)$. Rewriting (8.2) gives

$$\gamma(q_G G_- - R) + \delta U(G(q_G G_- - R), R) - K r_i$$

and because U_R is a deterministic constant, maximizing this payoff w.r.t. r_i makes $q_G G_- - R$ a constant, say ξ . This gives $\partial r_i / \partial G_- = q_G / Dn$ and U becomes:

$$\begin{aligned} U(G_-, R_-) &= \gamma(\xi) - K r + \delta U(G(\xi), R) \\ &= \gamma(\xi) - K \left(\frac{q_G G_- - \xi - q_R R_-}{Dn} \right) + \delta U(G(\xi), q_G G_- - \xi) \Rightarrow \\ m/\delta &= \partial U / \partial G_- = -K \left(\frac{q_G}{Dn} \right) + \delta U_{RqG} = -\frac{K q_G}{Dn} (1 - \delta q_R), \end{aligned} \quad (8.4)$$

since $G(\xi + \theta)$ and $\gamma(\cdot)$ are *not* functions of G_- when $q_G G_- - R = \xi$.

Since U_G is a constant, (8.1) implies that if R increases, y_i increases but G must decrease. Thus, $\partial y_i / \partial R \in (0, 1)$, so $\partial g_i / \partial R_j = \partial (y_i - R_i) / \partial R_j > 0$ if $i \neq j$ and < 0 if $i = j$. More precisely, differentiating (8.1) w.r.t. R or R_i gives:

$$\begin{aligned} B'' \frac{dy_i}{dR} - C'' \frac{n dy_i - dR}{dR} &= 0 \Rightarrow \\ \frac{dy_i}{dR} &= \frac{C''}{nC'' - B''} \Rightarrow \\ \frac{dg_i}{dR_i} &= \frac{C''}{nC'' - B''} - 1 = -\frac{C''(n-1) - B''}{nC'' - B''} < 0, \\ \frac{dg_i}{dR_j} &= \frac{C''}{nC'' - B''} > 0, j \neq i. \end{aligned}$$

Since $q_G G_- - R$ is a constant, when investments are symmetric (4.11)-(4.12) follow.

The first-order condition for R_i can be written (using (8.1)):

$$B'(y_i) \frac{dy_i}{dR} - [C'(G) - \delta U_G] \left[n \frac{dy_i}{dR} - 1 \right] + \delta U_R = K \Rightarrow$$

$$\begin{aligned}
B'(y_i) \left[\frac{dy_i}{dR} - n \frac{dy_i}{dR} + 1 \right] &= K - \delta U_R \Rightarrow \\
B'(y_i) \left[\frac{C''' - B''}{nC''' - B''} \right] &= (1 - \delta q_R/n) K.
\end{aligned} \tag{8.5}$$

For a given y_i , the left-hand side is smaller and the right-hand side larger than the first best (4.2). Thus, y_i must be smaller than the y_i satisfying (4.2). But since i consumes more than optimally *for a given R* , R must be lower than in the first best. Combined, the pollution level G must be larger than in the first best. By combining (8.5) and (8.1), we can write:

$$C' = B' + \delta U_G = (1 - \delta q_R/n) K \frac{nC''' - B''}{C''' - B''} + \delta U_G,$$

which is clearly larger than the first best (4.3), since U_G is the same in the two cases.

Proofs of Propositions 4-6.

When g_i is already negotiated, i invests until

$$K = dB'(g_i + R_i) + Dz \Rightarrow \tag{8.6}$$

$$y_i = B'^{-1}(K/d - Dz/d), \quad R_i = B'^{-1}(K/d - Dz/d) - g_i,$$

$$dr_i = B'^{-1}(K/d - Dz/d) - g_i - q_R R_{i,-} - \sum_{j \in N \setminus i} e r_j. \tag{8.7}$$

Anticipating this, the utility before investing is:

$$U_i = B(B'^{-1}(K/d - Dz/d)) - C(G) - K r_i + \delta U(G, R).$$

If the negotiations fail, the default outcome is the noncooperative outcome, giving everyone the same utility. Since the r_i s follow from the g_i s in (8.7), everyone understands that negotiating the g_i s is equivalent to negotiating the r_i s. Since all countries have identical preferences w.r.t. the r_i s (and their default utility is the same) the r_i s are going to be equal for every i . Symmetry requires that r_i , and thus $\zeta \equiv [g_i + q_R R_{i,-}]$, is the same for all countries. Then, (8.7) becomes

$$Dr_i = B'^{-1}(K/d - Dz/d) - \zeta.$$

Efficiency requires (f.o.c. of U_i w.r.t. ζ recognizing $g_i = \zeta - q_R R_{i,-}$ and $\partial r_i / \partial \zeta = -1/D \forall i$):

$$\begin{aligned}
-nC'(G) + K/D + n\delta U_G - nD\delta U_R(1/D) &= 0 \Rightarrow \\
C'(G) + m + zD &= K/Dn.
\end{aligned} \tag{8.8}$$

Combined with (8.7), neither G nor R can be functions of R_- (R_i in (8.7) and G in (8.8) are not functions of R_-). Thus, $U_{R_-} = q_R K / Dn$, just as before, and U_G cannot be a function of R (since $U_{RG} = 0$). (8.8) then implies that G is a constant and, since we must have $\zeta = (G - q_G G_-) / n + q_R R_- / n$, (8.7) gives $\partial r_i / \partial G_- = (\partial r_i / \partial g_i) (\partial g_i / \partial \zeta) (\partial \zeta / \partial G_-) = q_G / Dn$. Hence, $U_{G_-} = -q_G K / Dn + \delta U_R q_G = -q_G (1 - \delta q_R) K / Dn$, giving a unique equilibrium, (8.3) and (8.4), just as before.

Substituted in (8.8):

$$C'(G) = (1 - \delta q_G) (1 - \delta q_R) K / Dn. \quad (8.9)$$

This is the same pollution level as in the first best (4.3). At the same time, for a given g_i , equilibrium investments (8.6) are less than the first best investments (4.2). Thus, ex post the marginal benefit of polluting is larger than the marginal cost. Anticipating the ex post small g_i , r_i increases: from (8.7), $\partial r_i / \partial g_i = -1$. Combining (8.9) with (8.6),

$$B'(g_i + R_i - \bar{y}_i) / n - C'(G) - m = \frac{K}{n} \left(\frac{1}{d} - \frac{1}{D} \right) + \frac{\delta q_R K}{Dn} \left(1 - \frac{D}{dn} \right) =$$

$$\frac{K}{Dn} \left(\frac{1}{1 - (n-1)e/D} - 1 + \delta q_R \left(\frac{(D-en)(n-1)}{Dn-en(n-1)} \right) \right) = \frac{K}{Dn} \left(\frac{e + \delta q_R (D/n - e)}{D/(n-1) - e} \right).$$

For the quadratic functions, $B' = b(g_i + R_i - \bar{y}_i)$ and $C' = c(q_G G_- + \sum_i g_i)$, so

$$(B'/n - C')^{lt} - (B'/n - C')^* = b(-g_i^{lt} + g_i^*) / n - cn(g_i^{lt} - g_i^*) \Rightarrow$$

$$g_i^* - g_i^{lt} = \frac{K/D}{b + cn^2} \left(\frac{e/D + \delta q_R (1/n - e/D)}{1/(n-1) + e/D} \right).$$

Proofs of Propositions 7-9.

At the start of $t = 1$, countries negotiate emission levels for every period $t \in \{1, \dots, T\}$. The investment level in period T is (8.7) for the same reasons as given above.

Anticipating the equilibrium $R_{i,T}$ (and $R_{j,T}$) i can invest q_R less units in period T for each invested unit in period $T - 1$. Thus, in period $T - 1$, i invests until:

$$K = dB'(g_{i,T-1} + R_{i,T-1}) + \delta q_R K \Rightarrow \quad (8.10)$$

$$R_{i,T-1} = q_R R_{i,T-1} + dr_{i,T-1} + \sum_{j \in N \setminus i} er_{j,T-1} = B'^{-1}(K(1 - \delta q_R)/d) - g_{i,T-1}. \quad (8.11)$$

The same argument applies to every period $T - t$, $t \in \{1, \dots, T - 1\}$, and the investment level is given by the analogous equation for each period but T .

In equilibrium, all countries enjoy the same y_i and default utilities. Thus, just as before, they will negotiate the $g_{i,t}$ s such that they will all face the same cost of investment in equilibrium. Thus, $r_i = r_j = r$ and

$$Dr = B'^{-1} (K (1 - \delta q_R) / d) - g_{i,t} - q_R R_{i,t-1}.$$

For every $t \in (1, T)$, $R_{i,t-1}$ is given by the $g_{i,t-1}$ in the previous period (in line with (8.11)). Thus,

$$\begin{aligned} Dr &= B'^{-1} (K (1 - \delta q_R)) - g_{i,t} - q_R (B'^{-1} (K (1 - \delta q_R) / d) - g_{i,t-1}) \\ &= (1 - q_R) B'^{-1} (K (1 - \delta q_R)) - g_{i,t} + q_R g_{i,t-1}. \end{aligned} \quad (8.12)$$

Since $r_i = r_j$, (8.10) implies that the equilibrium $g_{i,t} + q_R R_{i,t-1}$ is the same (say ς_t) for all i s:

$$g_{i,t} + q_R^{t-\tau} R_{i,\tau-1} = \varsigma_t, \quad t \in \{1, \dots, T\}.$$

All countries have the same preferences over the ς_t s. Dynamic efficiency requires that the countries are not better off after a change in the ς_t s (and thus the $g_{i,t}$ s), given by $(\Delta \varsigma_t, \Delta \varsigma_{t+1})$, such that G is unchanged after two periods, i.e., $\Delta \varsigma_t q_G = -\Delta \varsigma_{t+1}$, $t \in [1, T - 1]$. From (8.12), this implies

$$\begin{aligned} -nC' (G_t) \Delta \varsigma_t + \Delta g_t K/D + \delta (\Delta \varsigma_{t+1} - \Delta g_t q_R) K/D - \delta^2 \Delta g_{t+1} q_R K/D &\leq 0 \forall \Delta \varsigma_t \Rightarrow \\ (-C' n + K/D - \delta (q_G + q_R) K/D + \delta^2 q_G d_R K/D) \Delta \varsigma_t &\leq 0 \forall \Delta \varsigma_t \Rightarrow \\ -C' n + (1 - \delta q_R) (1 - \delta q_G) K/D n &= 0. \end{aligned}$$

Using (8.10),

$$\begin{aligned} B' - C' (G) n - nm &= (1 - \delta q_R) K/d - (1 - \delta q_R) (1 - \delta q_G) K/D - \delta q_G (1 - \delta q_R) K/D \\ &= \frac{K (1 - \delta q_R)}{d} - (1 - \delta q_R) K/D = \left(\frac{K}{d} - \frac{K}{D} \right) (1 - \delta q_R) = \frac{K}{D} \left(\frac{e/D}{1/(n-1) - e/D} \right) (1 - \delta q_R). \end{aligned}$$

The $g_{i,T}$ satisfies (8.9) for the same reasons as in the previous proof (and since they do not influence any $R_{i,t}$, $t < T$). It is easy to check that U_R and U_G are the same as before.

Proofs of Propositions 10-12.

In the default outcome, a country's (interim) utility is:

$$W_i^{de} = B(g_i^{de} + R_i) - C\left(\tilde{G} + \sum_N g_j^{de}\right) + \delta U.$$

Since i gets $1/n$ of the renegotiation-surplus, in addition, i 's utility is:

$$W_i^{de} + \frac{1}{n} \sum_N (W_j^{re} - W_j^{de}) - Kr_i, \quad (8.13)$$

where W_j^{re} is j 's utility after renegotiation. Maximizing the expectation of this expression w.r.t. r_i gives the f.o.c.

$$\begin{aligned} K = & [dB'(g_i^{de} + R_i - \bar{y}_i) + Dz](1 - 1/n) + \\ & + \frac{D}{n} \partial \left(\sum_N W_i^{re} \right) / \partial R - \sum_{j \in N \setminus i} \frac{1}{n} [eB'(g_j^{de} + R_j) + Dz]. \end{aligned} \quad (8.14)$$

Clearly, R_i must decrease in g_i^{de} . Requiring first-best investments, $\partial(\sum W_i^{re})/\partial R = K/D$, and since $B'(g_i^{de} + R_i - \bar{y}_i)$ must be the same for all i s,

$$K = B'(g_i^{de} + R_i^*) (d - D/n) + K/n \Rightarrow B'(g_i^{de} + R_i^*) = \frac{K(n-1)}{dn - D}. \quad (8.15)$$

Combined with the optimum, (4.2),

$$\begin{aligned} B'(g_i^{de} + R_i^*) - B'(g_i^* + R_i^*) &= \frac{K(n-1)}{dn - D} - \frac{K}{D} (1 - \delta q_R) \\ &= \frac{K}{D} \left(\frac{e/D}{1/n - e/D} + \delta q_R \right). \end{aligned} \quad (8.16)$$

Since y_i^{de} is the same for every i in equilibrium, the bargaining game (when renegotiating the g_i^{de} s) is symmetric and the renegotiated g_i^{re} s become efficient (just as under short-term agreements). Since the first best is implemented, U_R and U_G are unique and as before.

Proof of Proposition 13.

The fact that Proposition 13 describes one equilibrium is easy to check. Uniqueness is not claimed for this case: while there cannot be inefficient equilibria (since all countries strictly prefer to negotiate an efficient contract), multiple contracts can implement the first best. For example, any contract specifying every $g_{i,t}$, $t \in \{1, \dots, T\}$, implements the

first best as long as $g_{i,1}$ is equal to g_i^* and the contract can be renegotiated already in the second period. The level of $g_{i,t}$, $t > 1$, is then not important. If $g_{i,t} \neq g_i^*$ and $T > t > 1$, the $g_{i,t}$ s will be renegotiated (to g_i^*) before period t .

Proof of Proposition 14.

The proposition follows from those above, since technological spillovers are allowed in all proofs.

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